

Defense of the Bachelor thesis:

# Optimization options for the usage of forecast combinations

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# Structure

1. *Forecast combination: motivation and application*

2. *Optimization approaches*

3. *Implementation*

4. *Results*

5. *Conclusion*



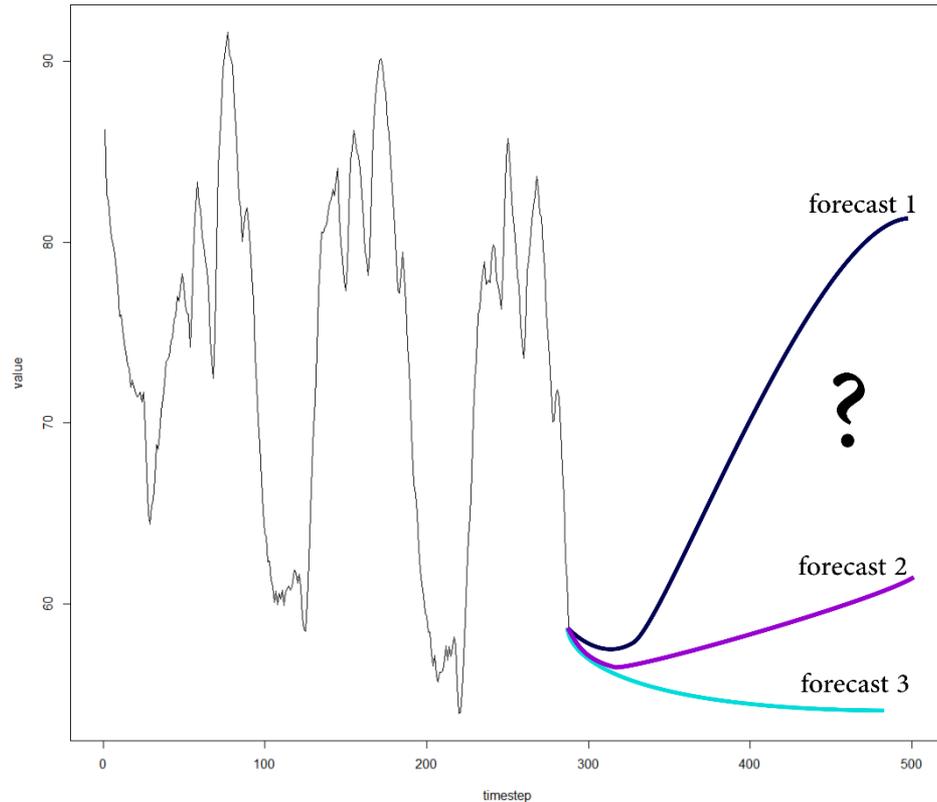
# Forecast combination: motivation and application

# Use cases

## Energy consumption

## Generation of solar energy

- Idea: use characteristics of several forecasting models at once
- Alternative to model selection



# General approach

## Combination techniques

- Naive methods: average / median of all values for each time step
- More complex methods: weights are assigned to each forecast

$$C_T = \sum_{i=0}^N k_i * f_{i,T}$$

$C_T$  - result of combination at time t

N - number of forecasts

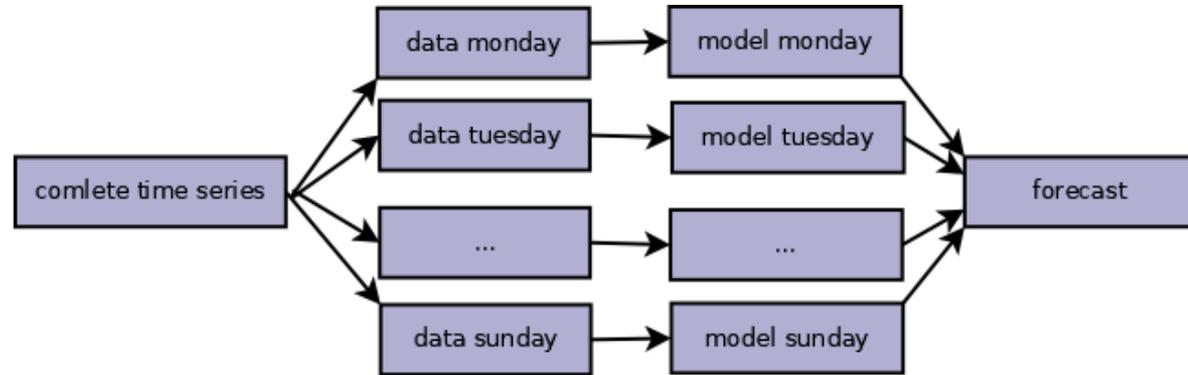
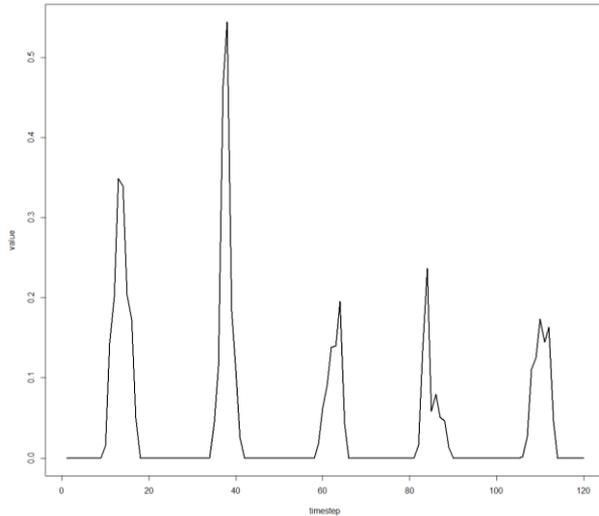
$k_i$  - weight of forecast i

$f_{iT}$  - forecast i at time t

# Optimization options

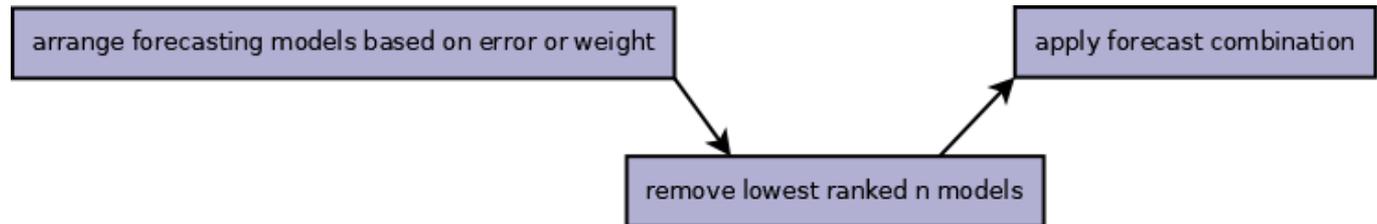
# Seasonal filtering

- *Idea: create several combination models for different seasonalities*
- *Assumption: forecast models show differences in their quality for different seasonalities*



# Exit of experts

- *Problem: limit the impact of weak forecast models on the combination*
- *Use of less forecast models based on their error*
- *Only models with a high quality are used*



# Implementation

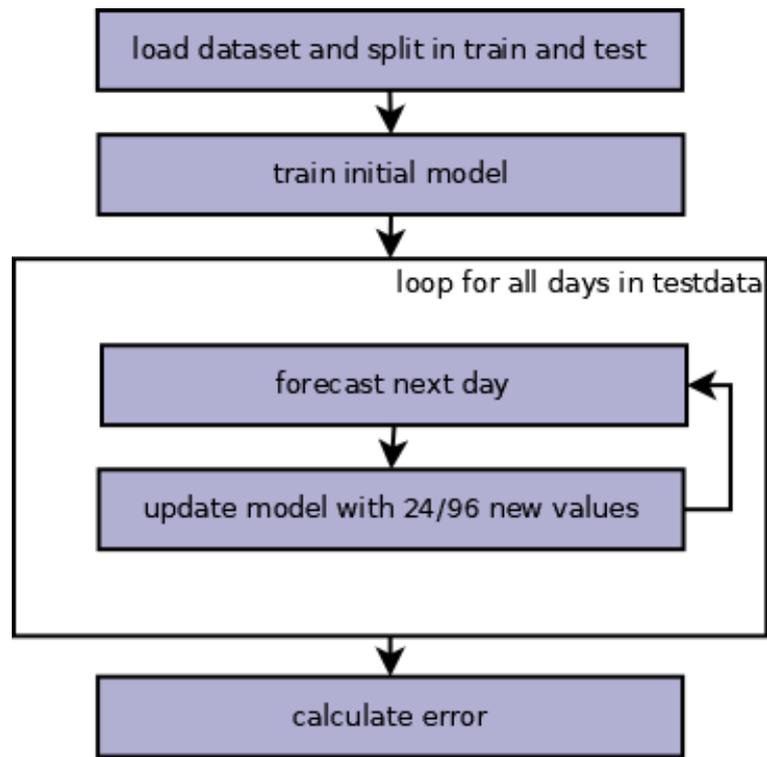
# Datasets and algorithm

## General approach

- Implementation in R
- Main focus on day-ahead forecast

## Datasets

- Energy consumption: aggregated consumption of the Swiss canton of Valais every 15 minutes (2015 and 2016) - 70276 observations
  - 6 forecasts
- Production of solar energy: hourly generation in Germany, Denmark and Australia (2013/2015) - 8760 observations each
  - 15 forecasts



# Combination techniques

## *Simple mean*

- Average of all given values without weights

## *Linear Regression*

- Using the `lm()`-package in R

## *L-BFGS-B*

- Quasi-Newton-method using the `optim()`-package in R

## *Bayesian model averaging*

- Probabilistic method

## *Opera-package for R*

- Contains five methods
- Domain: energy consumption

# Optimizations

## *Seasonal filtering:*

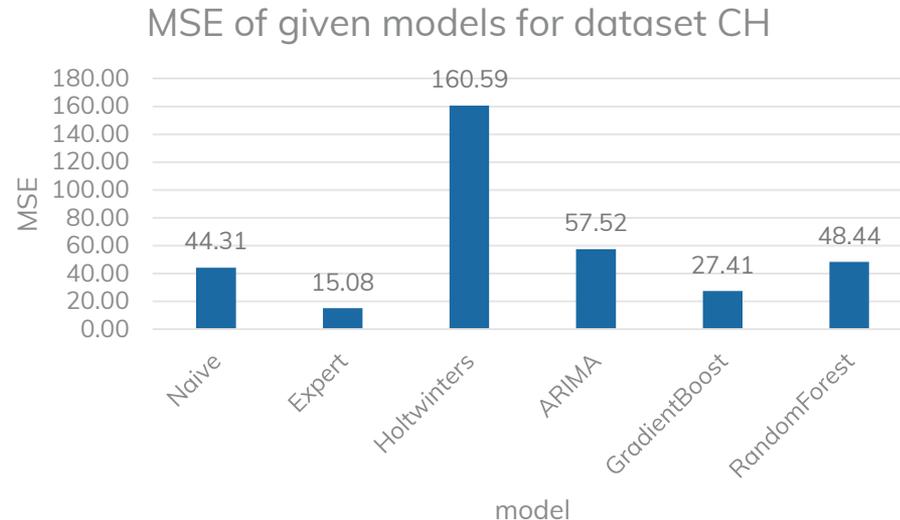
- Month of year (only for energy consumption)
- Day of week
- Hour of day

## *Exit of experts:*

- Remove 50% of the models...
- ...based on error (MSE)
- ...based on assigned weight

# Expectations

- Models differ in their quality: complex combination techniques should be superior to the simple mean
- Exit of experts should improve the quality of the forecast combination
- Seasonal Filtering should work especially well on an hourly level



# Error measures

absolute:

$$MSE = \frac{1}{N} \sum_{t=1}^N (F_t - A_t)^2$$

percentage:

$$SMAPE = \frac{100\%}{N} \sum_{t=1}^N \frac{|F_t - A_t|}{(|A_t| + |F_t|)/2}$$

# Results

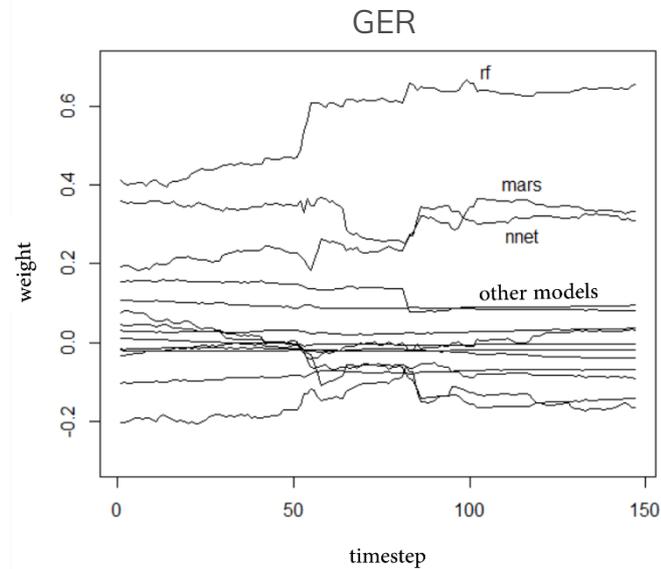
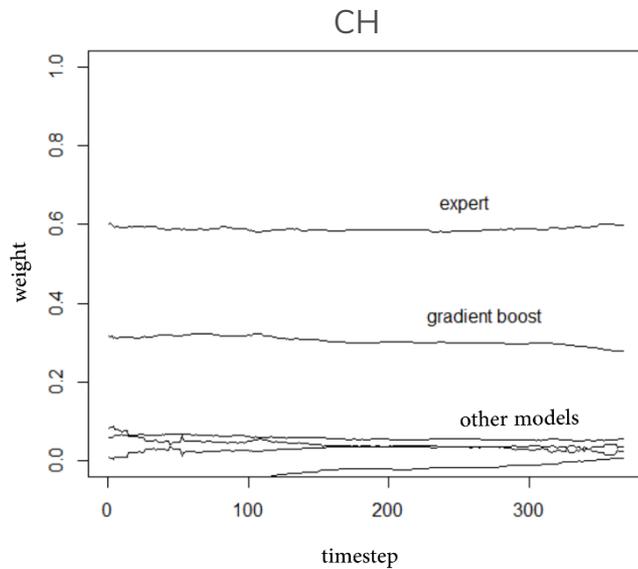
# Combination methods

- Linear regression and bayesian model averaging showed the best results (regression as basis for further optimizations)
- Methods of opera-package better for one-step-ahead forecast for energy consumption

SMAPE	CH	GER	AUS	DEN
Best single model	6,66%	44,26%	16,05%	45,30%
Simple mean (improvement)	6,06%	44,28%	172,28%	37,38%
Linear Regression (improvement)	-18,65%	18,34%	-29,45%	-7,55%
Bayesian model averaging (improvement)	-18,65%	18,88%	-30,79%	-8,58%

# Solar data

- Unstable results for solar data
- Fluctuating quality of the given forecast models



# Exit of experts

- Removing based on error often leads to worse results
- Removing based on weights can lead to a smaller error
- Mostly just slight changes

SMAPE	Linear regression	Exit based on weights (improvement)	Exit based on error (improvement)
CH	5,42%	0,44%	2,42%
GER	52,32%	-0,31%	-0,36%
AUS	11,33%	-0,18%	0,93%
DEN	41,88%	0,26%	0,37%

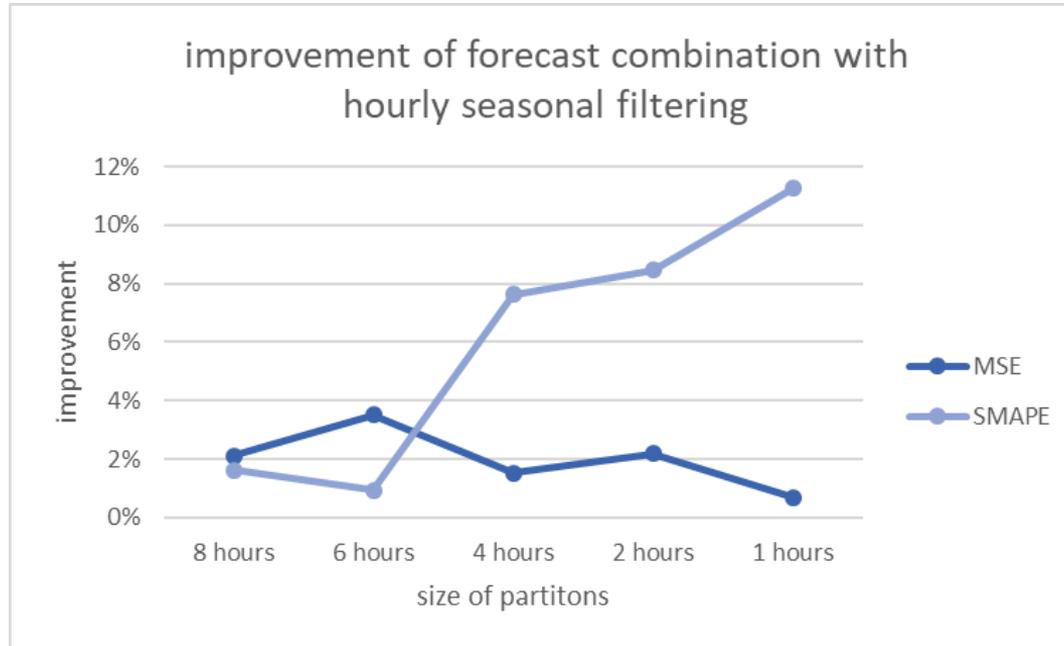
# Seasonal Filtering

- Filtering for month of year with a slightly higher error
- Filtering for day of week just suitable for energy consumption
- Filtering for hour of day improves the result of the combination in most cases

SMAPE	CH	GER	AUS	DEN
Lin. Regression	5,42%	128,30%	95,85%	164,88%
Season (improvement)	1,17%	Not applicable		
Weekday/Weekend (improvement)	-0,63%	0,01%	0,03%	0,10%
24 hours (improvement)	-7,24%	-0,67%	-32,57%	-4,56%

# Seasonal filtering

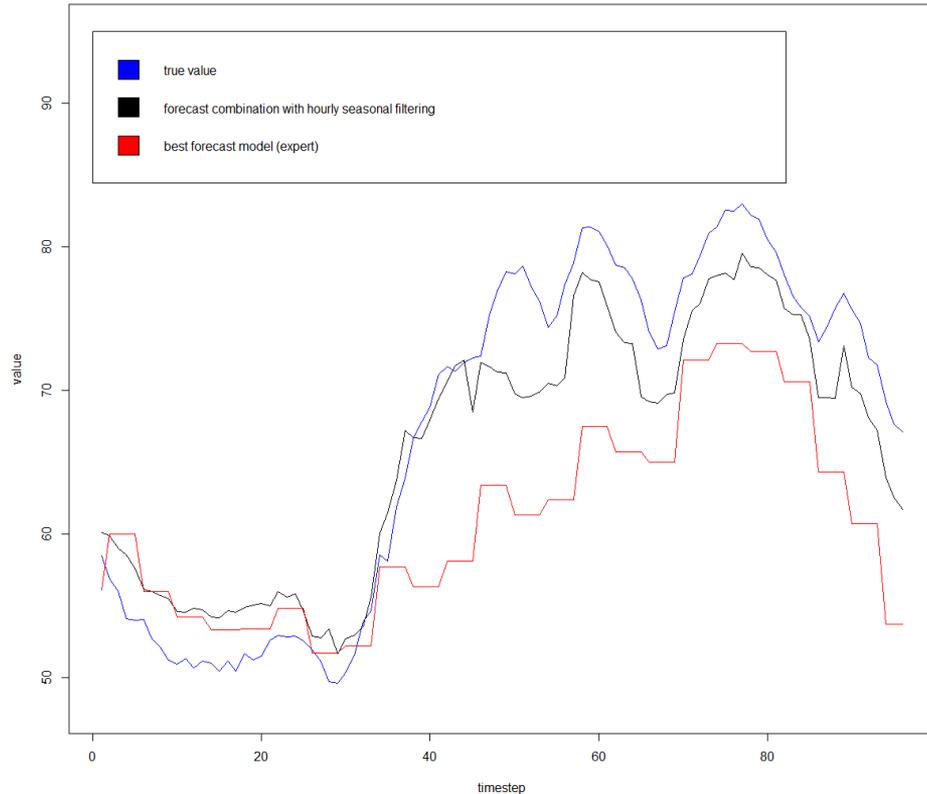
- Principle: The smaller the partitions, the better the result



# Conclusion

# Findings

- Seasonal filtering has the potential to improve the results of forecast combinations
- Recommended especially on an hourly level
- Exit of experts can be successful, but naive approach is not good enough
- BUT: combination for solar data partly with a higher error than best forecast model



# Future approaches

## *Forecast of optimal combination weights for the next day*

- Overcome the naive method of using the optimal weights of the previous day

## *More complex method for the exit of experts*

- Time-dependent entry and exit

## *External influences*

- E.g. weather data

## *Evaluation with other error measures*

- MSE and SMAPE showed major differences